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## 1.I BRARY

## - NIVERSITY OF ILAFORNIA.

## Life Insurance

## Premiums and Reserves.



BY<br>SHEPPARD ${ }_{\|}$HOMANS,<br>Consulting Actuary.

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## Life Insurance Premiums and Reserves.

BY SHEPPARD HOMANS; CONSULTING ACTUARY.

The basis of every sound system of life insurance is the Mortality Table. While nothing is more uncertain than the duration of an individual life, the rates of mortality, or, in other words, the probabilities of living and dying in any one year at each age among a large number of persons similiarly situated as regards family history, climatic influences, etc., can be predicted with almost mathematical precision. The rates of mortality among insured lives at the several ages have been carefully ascertained by observations among a vast number of persons insured in British and American companies. These results are embodied in three mortality tables of standard authority, viz:

The Actuaries, or Combined Experience Table, deduced from the mortuary statistics of seventeen British companies, and published in 1837.

The New Actuaries or Hm. Table, deduced from the later experience of twenty British companies, and published in 1869.

The American Experience Table, deduced chiefly from the mortuary statistics of the Mutual Life Insurance Company of New York.

Of these the last named table, confirmed, as it has been in a remarkable degree, by the experience of other American companies, is by far the best index of the rates of mortality which may be expected to prevail among insured lives in the United States. This table has been adopted by nearly all American companies as a basis for premiums and reserves, and by mâny States as a standard of valuation for contingent insurance liabilities.

These tables do not differ materially from each other, and either would be a safe basis for the transactions of American life insurance companies. Their teachings have all the force of natural laws, and these teachings cannot be disregarded or violated with impunity.

Columns (I) and (2) of the following Table No. I, show respectively the numbers living and dying at each successive age out of 100,000 persons starting at the age of ten years. Column (3) shows for each age the rate of mortality, or probability of dying within one year. This is also the cost, without interest, to insure one dollar, or unity, payable in case of death within the year, and is found, for any age, by dividing the number of deaths by the number living. For instance, at age 40 , dividing 765 , the number dying, by 78,106 , the number living, we have . 009794 as the

Table No. I .

| $\underset{x}{A g}$. | Number Living at Each Age. <br> $l_{x}$ | Number Dying at Each Age. <br> $d x$ | Probability of Dying at Each Age, Which is Also the Cost to Insure $\$ 1.00$ for One Year, at Each Age.$\frac{d x}{l_{x}}$ | Probability of Living 'Through the Year at Each Age.$1-\frac{d x}{l_{x}}$ | Cost to Insure \$1,000 Payable in case of Death. Am. Exp. $4 \%$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | For One Year Only, at Age $x$ | Equal Yearly Premiums Dur ing Remainder of Life. |
|  | (1) | (2) | (3) | (4 | (5) | (6) |
| Io | 100,000 | 749 | . 007490 | 992510 | 720 | 10.53 |
| 11 | 99,250 | 746 | . 007516 | 992484 | 7.23 | 10.70 |
| 12 | 98,505 | 743 | . 007543 | 992457 | 7.25 | 10. 88 |
| 13 | 97,762 | 740 | . 007569 | 99243I | 7.28 | 11.06 |
| 14 | 97,022 | 737 | . 007596 | . 992404 | 7.30 | II. 26 |
| 15 | 96,285 | 735 | . 007034 | . 992366 | 7.34 | II. 47 |
| 16 | 95.550 | 732 | . 007661 | . 992339 | $7 \cdot 37$ | 11. 69 |
| 17 | 94,818 | 729 | . 007688 | . 992312 | 7.39 | 11.91 |
| 18 | 94,889 | 727 | . 007727 | . 992273 | 7.43 | 12. 15 |
| 19 | 93,362 | 725 | . 007765 | . 992235 | 7.47 | 12.40 |
| 20 | $9^{2,637}$ | 723 | . 007805 | .992195 | 7.51 | 12.67 |
| 21 | $9 \mathrm{Cl}, 9 \mathrm{I} 4$ | 722 | . 007855 | . 992145 | 755 | 1295 |
| 22 | 91,192 | 721 | . 007906 | . 992094 | 7.60 | 13.24 |
| 23 | 90471 | 720 | . 007958 | .992042 | 7.65 | 13.55 |
| 24 | 89,751 | 719 | . 008011 | .991989 | 7.70 | 13.87 |
| 25 | 89.032 | 718 | . 008065 | . 991935 | 7.75 | It. 21 |
| 26 | 88.314 | 718 | .008130 | .991870 | 7.82 | 14.57 |
| 27 | 87.596 | 718 | . 008197 | .991803 | 7.88 | 14.95 |
| 28 | 86,878 | 718 | . 008264 | .991736 | 7.95 | 15.35 |
| 29 | 86,160 | 719 | . 008345 | .991655 | 8.02 | 15.77 |
| 30 | 85.44 T | 720 | . 008427 | .991573 | 8.10 | 16.21 |
| 31 | 84,721 | 721 | . 008510 | .991490 | 8.18 | 16.68 |
| 32 | 84,000 | 723 | . 008607 | .991393 | 8.28 | 17. 18 |
| 33 | 83,277 | 726 | . 008718 | . 991282 | 8.38 | 17.70 |
| 34 | 82,551 | 729 | . 008831 | .991169 | 8.49 | 18.26 |
| 35 | 81,822 | 732 | . 008946 | .991054 | 8.60 | 1884 |
| 36 37 | 81,090 | 737 | . 009089 | .990911 | 874 888 | 1946 |
| 37 <br> 38 <br> 8 | 80,353 | 742 749 | . 009234 | . 990766 | 8.88 905 | 20.12 |
| 39 | 78,862 | 756 | . 009586 | .990414 | 9.22 | 21. 57 |
| 40 | 78,106 | 765 | . 009794 | . 990206 | 9.42 | 22.35 |
| 4 I | 77,341 | 774 | . 010008 | . 989992 | 962 | 23.19 |
| 42 | 76,567 | 785 | . 010252 | . 989748 | 9.86 | 24.08 |
| 43 | 75,782 | 797 | . 010517 | . 989483 | 10.11 | 25.03 |
| 44 | 74,985 | 812 828 | . 010829 | .989171 | 10.41 | 26.04 |
| 45 | 74,173 73,345 | 828 848 | . .10111563 | . 98888338 | 10.73 II. 12 | 27.12 |
| 47 | 72,497 | 870 | . 012000 | . 988000 | II. 54 | 29.50 |
| 48 | 71,627 | 896 | . 012509 | . 987491 | 1203 | 30.81 |
| 49 | 70,731 | 927 | .013106 | . 986894 | 12.60 | 32.21 |
| 50 | 69,804 | 962 | .013781 | . 986219 | 13.25 | 33.70 |
| 51 | 68.842 | OOI | . 014541 | . 985459 | 13.98 | 35.29 |
| 52 | 67,841 | 1,044 | .015389 | . 984611 | 1480 | 36.98 |
| 53 | 66,797 | 1,091 | . 016333 | .983667 | 15.71 | 38.79 |
| 54 | 65,706 | I, I43 | .017396 | -982604 | 1673 | 40.73 |
| 55 56 | 64,563 63364 | I,199 I, 260 | . 0185719 | .981429 | 17.86 | 4279 |
| 57 | 62,104 | I, 325 | . 021335 | .978665 | 19.12 | 4735 |
| 58 | 60,779 | I,394 | . 022936 | . 977064 | 22.00 | 4987 |
| 59 | 59,385 | 1,468 | . 02472 n | .975280 | 2377 | 52.57 |
| 60 | 57.917 | 1,546 | . 026693 | . 973307 | 2567 |  |
| 61 | 56,371 | I,628 | . 228880 | . 971120 | 27.77 | 58.54 |
| 62 | 54,743 | 1,713 | .031292 | . 968708 | 30.09 | 6 6 .84 |
| 63 | 53.030 | 1,800 | . 033943 | . 966057 | 31.90 | 6539 |
| 64 | 51,230 | 1,889 | . 036873 | . 963127 | 3545 | 69.18 |
| 65 | 49,34I | 1,980 | . 040129 | -959871 | 3859 | 73.25 |
| 66 | 47,361 | 2,070 | . 043707 | . 956293 | 42.03 | 77.61 |
| 67 68 | 45,291 | 2,158 2,243 | . 047647 | . 9523533 | 45.82 50.00 | 82.28 87.29 |
| 69 | 43,13 40,890 | 2,32I | . 056762 | . 9442388 | 54.58 | 92.65 |
| 70 | 38,569 | 2.391 | . 061993 | . 938007 | 59.61 | 9839 |
| 71 | 36,178 | 2.448 | . 067665 | . 932335 | 65.06 | 104.54 |

Table No. I-Continued.

| Age. | Number Living at Each Age. <br> $l_{x}$ | Number Dying at Each Age. <br> $d x$ | Probability of Dying at Each Age. Which is Also the Ccst to Insure $\$ \mathbf{r} .00$ for One Year, at Each Age.$\frac{d x}{l_{\mathrm{x}}}$ | Probability of Living Through the Year at Each Age. $1-\frac{d x}{l_{x}}$ | Cost to Insure \$1,000 Payable in case of Death. Am. Exp. 4\%. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | For One Year Only, at Age $x$ | Equal Yearly <br> Premiums During Remainder of Life. |
|  | (1) | (2) | (3) | (4) | (5) | (6) |
| 72 | 33.730 | 2,487 | . 073733 | . 926267 | 70.90 | III. 13 |
| 73 | 3 I .243 | 2,505 | . 080178 | . 919822 | 77.09 | 118.21 |
| 74 | 28,738 | 2,501 | . 087028 | . 912972 | 83.68 | 125.85 |
| 75 | 26,237 | 2,476 | . 094371 | .905629 | 90.74 | 134.14 |
| 76 | 23,761 | 2,43I | . 1023 IT | . 897689 | 9838 | I43.19 |
| 77 | 21,330 | 2,369 | . 111064 | . 888936 | 106.79 | 153.14 |
| 78 | 18,961 | 2,291 | . 120827 | . 879173 | 116.18 | 164.12 |
| 79 | 16,670 | 2,196 | . 131734 | . 868266 | 126.67 | 176.30 |
| 80 | 14,474 | 2,OSI | . 144466 | . 855534 | 138.91 | 189.87 |
| 81 | 12,383 | 1,¢64 | . 158605 | . 841395 | 152.50 | 204.95 |
| 82 | 10,419 | 1, 816 | . 174297 | . 825703 | 167.59 | 221.82 |
| 83 | 8,603 | I,648 | .19156I | . 808439 | 184.19 | 240.90 |
| 84 | 6,955 | 1,470 | . 211359 | .78864I | 20323 | 262.89 |
| 85 86 | 5.485 | 1,292 | . 235552 | . 764448 | 226.49 | 288.62 |
| 86 87 | 4,193 | 1,114 | .26568I | . 734319 | 255.46 | 318.82 |
| 87 | 3,079 $\mathbf{2 , 1 4 6}$ | 933 744 | . 303020 | .696980 .653308 | 291.37 334.13 | 354.03 394.52 |
| 89 | 1,402 | 555 | - 39586 | . 604137 | 380.64 | 44 I .22 |
| 90 | 847 | 385 | . 454545 | . 545455 | 43706 | 497.08 |
| 9 I | 462 | 246 | . 532466 | . 467534 | 5 II 99 | 566.28 |
| 92 | 216 | 137 | . 634259 | . 365741 | 609.87 | 649.34 |
| 93 | 79 | 58 | . 734177 | . 255823 | 705.94 | 736.31 |
| 94 | 21 | I8 | . 857143 | . 142857 | 824.18 | 840.77 |
| 95 | 3 | 3 | 1.000000 | 0.000000 | 96154 | 96I. 54 |

rate of mortality or probability of dying within one year, at that age. Column (4) gives for each age the probability of surviving through one year. This is also the cost, without interest, to provide one dollar, or unity, at the end of one year, payable in case of surviving to the end of the year. This is found by dividing the number living at the next higher age, or one year older, by the number living at the age indicated. Thus for age 40 , the probability of surviving through one year is found by dividing 77,341 , the number living at age 4 I , by 78,106 , the number living at age 40 , and is represented by the fraction .990206 . This also is the value, without interest, of one dollar, or unity, payable in case a person now aged 40 is alive at the end of one year.

As it is certain that every individual will be either alive or dead at the end of the year, the probabilities of dying and of living in one year at age 40 may be represented as follows:

| Probability of dying in one year. | . 009794 |
| :---: | :---: |
| Probability of living through one year. | . 990206 |
| Certainty of living or dying in one year | 1.0000 |

Column (5) gives the cost, in advance, for each age to secure $\$ 1000$ payable at the end of the year in case of death within the year, assuming interest at four per cent
per annum. Thus, for age 40 , the sum of $\$ 9.42$ paid in advance is the net cost to secure $\$ 1000$ payable at the end of the year provided death should occur within the year. Similiarly at age 50 , the cost to insure $\$ 1000$ for one year is $\$ 13.25^{\text {. }}$. At age $60, \$ 25.67$; at age $70, \$ 59.6 \mathrm{r}$, etc. This cost of insurance for one year is, of course, independent of the form of policy contract, or of the age at which the policy was issued, and in general increases each year as a man grows older. These yearly increasing costs of insurance are called natural premiums.
$\angle$ It may be laid down as a fundamental principle that every life insurance company must collect each year, in some way, either by direct payments, or partly from an accumulated fund and partly by direct payments, the cost, according to these natural premiums, to cover the insurance for the year of the net amount at risk on each and every policy in force, based upon the actual age attained, regardless of the age at entry, the form of policy contract, or the scale of premium payments. $\rangle$

These natural premiums, or cost of insurance for each separate year, constitute the basis of all sound life insurance. Theoretically, the receipt each year of the natural premium, or yearly cost of insuring the net amount at risk, based always upon the actual age attained, will enable any company to meet all its insurance obligations at maturity, on each and every policy in force. Practically, it is necessary to add, under any form of policy contract, a margin for necessary expenses, and a further margin to guard against adverse contingencies, such as epidemics, undue withdrawal of sound lives, etc. But it cannot be too clearly stated that natural premium payments, properly loaded, are not only sufficient, but are all-sufficient to meet all the insurance obligations of any company, no matter what may be the forms of its policy contracts or the methods of its premium adjustments. In fact, any payment in excess of the natural premium applied to the net amount at risk and to the actual age attained is outside of, and independent of, insurance, and should go to expenses, contingent fund, investment or surplus. The natural premium in any year pays for the entire insurance during that year, under any and every form of policy contract in any and every company.

Column (6) gives for each age the level or uniform premiums, to continue unchanged through the remainder of life, as the consideration for securing \$1000 payable at the end of the year when death occurs. For instance, at age 40 the payment of $\$ 22.35$. annually in advance is the net premium at that age to secure $\$ 1000$, payable at the end of the year when death occurs. These level premiums are the commuted equivalents of the natural, or increasing premiums, as shown in column (5).

We will now examine the principles upon which these level premiums are determined.
$\angle$ The first step is to ascertain the net single premium or amount to be paid down in one sum to secure $\$ 1000$ payable at death, whenever that event shall happen. It is manifest that this single premium is the sum total of the separate costs of insuring one dollar, or unity, in each successive year, discounted at the rate of interest assumed to the present date or age. As we have seen, the net cost without interest at age 40 1888 OB Homans Life Insurance Premium and Reserves 20p bonknote

Table No. 2.

| Age. $40+n$ |  |  |  |  |  |  | $n$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) | (4) | (5) | (6) |  |
| 40 | . 009794 | .961538 | .0094177 | 1.000000 $\times$ | 1.000000 | 1.00000 $=$ | $\bigcirc$ |
| 41 | . 009910 | . 924556 | .0091620 | . 990206 | .961538 | . 95212 | 1 |
| 42 | . 010050 | . 888996 | . 0089348 | . 980296 | . 924556 | . 90634 | 2 |
| 43 | . 010204 | . 854804 | . 0087225 | . 970246 | . 888996 | . 86254 | 3 |
| 44 | . 010396 | . 821927 | . 0085449 | -96co42 | . 854804 | . 82065 | 4 |
| 45 46 | .010601 | .790315 .759918 | .0083781 | . 949645 | . 8219027 | . 78054 | 5 6 |
| 47 | .OIII39 | .730690 | .0081389 | . 928187 | .759918 | . 70535 | 7 |
| 48 | .011471 | . 702587 | . 0080598 | .917049 | .730690 | . 67008 | 8 |
| 49 | .011869 | . 675564 | .0080179 | .905577 | . 702587 | . 63625 | 9 |
| 50 | . 012317 | .64958I | . 0080006 | . 893709 | . 675564 | . 60376 | 10 |
| 51 | . 012816 | . 624597 | . 0080048 | .88I392 | . 649581 | . 57254 | II |
| 52 | .013366 | . 600574 | . 0080275 | . 868576 | . 624597 | . 54201 | 12 |
| 53 | .or3968 | . 577475 | . 0080663 | .855212 | . 600574 | . 51362 | 13 |
| 54 | . 1014634 | -555265 | .0c81257 | . 841241 | . 577475 | . 48580 | 14 |
| 55 | . 015351 | . 533908 | .008I960 | . 826606 | . 555265 | -45899 | 15 |
| 56 | .016132 | .513373 | .0082817 | .811257 | . 533908 | .43314 | 16 |
| 57 | .016964 | . 493628 | . 0083740 | . 795125 | . 513373 | -40820 | 17 |
| 58 | . 017848 | . 474642 | . 00847712 | .778160 | . 493628 | . 38412 | 18 |
| 59 | . 018795 | . 456387 | . 0085778 | .760313 | -474642 | . 36088 | 19 |
| 60 | . 019794 | . 438834 | .008686I | .741518 | -456387 | . 33842 | 20 |
| 6 I | . 020843 | . 421955 | . 0087950 | . 721724 | . 438834 | -31672 | 21 |
| 62 | .021932 | . 405726 | . 0088983 | .700881 | . 421955 | . 29574 | 22 |
| 63 | . 023046 | .390121 | . 0089906 | . 678949 | . 405726 | . 27547 | 23 |
| 64 | . 024185 | . 375117 | .0090722 | . 655904 | -390121 | . 25588 | 24 |
| 65 | . 025350 | . 360689 | .0091435 | . 631718 | -375117 | . 23697 | 25 |
| 66 | . 026502 | -346817 | .0091915 | . 606367 | . 360689 | .21871 | 26 |
| 67 | . 027629 | . 333477 | .009213I | . 579866 | .346817 | . 20111 | 27 |
| 68 69 | .028762 .029716 | .320651 | .0092083 ${ }^{\text {. }}$ | .552237 .523519 | .333477 .320651 | . 18416 | 28 29 |
|  | . 029716 | -308319 | . 0091620 | . 523519 | . 320651 | . 16787 | 29 |
| 70 | .0306I2 | . 296460 | .0090753 | . 493803 | . 308319 | . 15225 | 30 |
| 71 | .03I342 | . 285058 | . 0089343 | .463191 | . 296460 | . 13732 | 31 |
| 72 | .031841 | . 274094 | . 0087275 | . 431849 | . 285058 | . 12310 | 32 |
| 73 | .032072 | $.26355^{2}$ | . 0084526 | - 400008 | . 274094 | .10964 | 33 |
| 74 | . 332021 | . 253415 | .0081145 | . 367936 | . 263552 | . 09697 | 34 |
| 75 | .031701 | . 243669 | . 0077244 | -335915 | . 253415 | . 08513 | 35 |
| 76 | . 031124 | . 234297 | . 0072923 | -303515 | . 243669 | . 07413 | 36 |
| 77 | .03033I | . 225285 | .0568330 | . 273090 | . 234297 | .06398 | 37 |
| 78 79 | .029332 | .216621 .208289 | . 0063539 | . 242760 | . 225285 | . 05469 | 38 |
| 79 | .028I16 | . 208289 | . 0058562 | .213428 | .21662I | . 04623 | 39 |
| 80 | .026771 | . 200278 | .0053617 | .185312 | . 208289 | .03860 | 40 |
| 8 81 | . 025145 | . 192575 | . 0048424 | . 158541 | . 200278 | .03175 | 41 |
| 82 | . 023250 | . 185168 | . 0043052 | . 133396 | . 172575 | . 02569 | 42 |
| 83 | . 021100 | . 178046 | . 0037567 | . 110145 | . 185168 | . 02040 | 43 |
| $8{ }_{8}^{85}$ | . 018821 | . 171198 | .0032221 | .089こ46 | . 178046 | . 01585. | 44 |
| 85 80 | . 016542 | . 164614 | . 0027232 | . 070225 | . 171198 | .01202 | 45 |
| 87 | . 01.1946 | . 152295 | . 0021875180 | . 0533684 | .164614 | . 008684 | 46 |
| 88 | . 009526 | .14634I | . 0013940 | . 027476 | . 152295 | .00418 | 48 |
| 89 | . 007106 | . 140713 | .00c9999 | .017950 | .14634I | . 00263 | 49 |
| 90 | .004929 .003150 | . 135301 | $.0006669$ | .010844 | . 140713 |  | 50 |
| 91 92 | .003150 .001754 | . 130097 | .0004097 .0002194 | . 0002715 | . 135301 | .00080 | 51 52 |
| 93 | . 000743 | . 120282 | . 0000893 | . 0 IOII | . 125093 | .00013 | 53 |
| 94 | . 000230 | .II5656 | . 0000267 | . 000269 | . 120282 | . 00003 | 54 |
| 95 | . 000038 | . 112207 | . 0000043 | . 000038 | . 115656 | . 00000 | 55 |
|  |  |  |  |  |  |  |  |
| Totals. |  | ..... | -3675747 | .......... | ......... | 16.443 II | . |

to secure $\$ \mathrm{r}$, payable at the end of one year in case of death during the first year, is .009794 . To find its net present value, paid down, we must discount this cost for one year at the rate of interest assumed. The present value of one dollar, payable certain at the end of one year, at four per cent interest, is .961538 . The net present value of one dollar, or unity, payable at the end of one year in case of death, on the basis of the American Table-four per cent interest-is for age 40 years $.009794 \times$ $.96{ }^{1} 538=.0094177$. [See columns (1), (2), and (3), Table No. 2.] In the same way the net present value of one dollar, or unity, payable at the end of two years, provided a person now aged 40 should die in the second year, or between ages 41 and 42 , is found by dividing 774 , the number dying, by 78,106 , the number living at age 40 , and discounting the quotient for two years. Thus ${ }_{78106}^{714}=.009910$; this multiplied by $92455^{6}=.0091620$, and this is the cost at age 40 to secure one dollar, or unity, payable at the end of two years in case of death during the second year. Again, the net present value of one dollar, payable in case a man now aged 40 years should he die in the eleventh year, or between ages 50 and 5 I , is . 00 Sooo6. These separate values are shown in column No. 3 in Table No. 2. Their sum total is .3675747 , and this is the net single premium paid down to secure one dollar, or unity, payable at the end of the year, when a person now aged 40 years dies, whenever that event shall happen.

By a similar course of reasoning the net present value of one dollar, or unity, payable annually in advance during the remainder of life at any age, is the sum total of the present values of the separate chances of surviving during each successive year, discounted to the present date or age. Thus for age 40 the present value of one dollar in advance is unity or one dollar. The present value, without interest, of one dollar, payable in one year, or at age 4 I , is, as we have seen, .990206 . This multiplied by .961538 , the discount, gives. 95212 as the present value of one dollar, payable at the end of one year, or at age 4 I , provided a person now aged 40 be then alive. The present value of one dollar, payable in ten years, or at age 50 , provided a person now aged 40 be then alive, is ${ }_{8}^{68806}=.893709$ multiplied by $.675564=.60376$. These successive net present values are found in column (6). Their sum total is $\mathbf{1 6 . 4 4 3 1 1}$, and this is the present value of one dollar per annum in advance during the lifetime of a person now aged 40 years upon the basis adopted.

As already shown, the net single premium at age 40 to secure one dollar, or unity, payable at the end of the year when death occurs, is .3675747 . Proportionally, a net single premium of $\$ \mathbf{r} 6.433^{1 I}$ would secure $\$ 44.734^{1}$ payable at death. But $\$$ I6.443II is also the net present value at age 40 of an annual premium of one dollar. Therefore, a net level or uniform premium of $\$ 22.3543$ would, at age 40 , secure \$1000 payable at death. [See column (6), Table No. i.]

Let us now suppose a company to consist of 78 , ro6 persons, each aged 40 years, each insured for $\$ 1000$, or $\$ 78,106,000$ in all, and each paying the net annual premium of $\$ 22.3543$. The following table No. 3 has been prepared to show the progress of the fund each year until the last death claim has been paid at the age of 96 years, on the basis of the American Experience Table and four per cent interest. Column

Table No. 3.
78, 106 Persons. Aged 40 Years, Insured for \$1,000 Each.

| Age. $x$ | Premiums. | Fund at Beginning of Year. | Interest 4\%. | Death Claims. | Fund at End of Year. | Share of Each Person in the Fund at End of <br> Year or Net Reserve. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 40 | $\begin{gathered} \text { (I) } \\ \$ \mathrm{t}, 746, \mathrm{c} 30 \end{gathered}$ | $\begin{gathered} (2) \\ \$ \mathrm{I}, 746,030 \end{gathered}$ | $\begin{gathered} (3) \\ \$ 69,8 .+0 \end{gathered}$ | $\begin{gathered} (4) \\ \$ 765,0>0 \end{gathered}$ | $(5)$ $\$ 1,050,870$ | (6) 3.59 |
| 4 | T.728,930 | 2,779,800 | III, IgO | 774,000 | 2,116.990 | 27.65 |
| 42 | 1.711,630 | 3,828,620 | 153,140 | 785,000 | 3,196,760 | 42 I8 |
| 43 | 1,694,080 | 4,890,840 | 195.630 | 797,000 | 4,289,470 | 57.20 |
| 41 | 1,676,260 | 5,965,73 | 238,630 | 812,000 | 5,392,360 | 7270 |
| 4.5 | 1,658,110 | 7,050,470 | 282,020 | 828,000 | 6,504,490 | 88.68 |
| 46 | 1,639,600 | 8, 144,090 | 325,760 | 848,000 | 7,621,850 | 10513 |
| 47 | I 620,640 | 9,242,490 | 369,700 | 870,000 | 8,742,190 | 122.05 |
| 48 | 1,601,190 | 10,343,380 | 413,740 | 896,000 | 9,861.120 | 139.42 |
| 49 | 1,581,170 | II,442,290 | 457,690 | 927,000 | 10.972,980 | I57.19 |
| 50 | I.560,440 | 12,533,420 | 501, 340 | 962,000 | 12,072,760 | 175.37 |
| 51 | 1,538,940 | 13,611,700 | 544,470 | 1 OOI,000 | 13,155,170 | 193.91 |
| 52 | 1.516,560 | 14,671,730 | 536,870 | I 044000 | - 14,214,600 | 212.80 |
| 53 | I,493,220 | 15,707,820 | 628,310 | 1,091,000 | 15,245, 130 | 232.02 |
| 54 | I, 468,830 | 16,713,960 | 668560 | 1,143.000 | 16,239,520 | 251.53 |
| 55 | I 443,290 | 17,682,810 | 707,310 | 1,199.000 | 17,191,120 | 271.30 |
| 5? | 1,416,480 | 18,607,600 | 744,300 | I 260,000 | 18,091,900 | 291.31 |
| 57 | 1,388310 | 19,480,210 | 779210 | 1,325,000 | 18.934,420 | 311.52 |
| 58 | 1,358,680 | 20,293,100 | 811 720 | 1,394,000 | $19.710,820$ | 331.91 |
| 59 | 1,327,520 | 21,038,340 | 841530 | 1,408,000 | 20411,870 | 352.43 |
| 60 | 1,244,710 | 21,706,580 | 868,260 | I 546,000 | 2I,028 840 | 373.04 |
| 61 | 1,260,150 | 22,288,990 | 891,560 | I,628,000 | 21,552,550 | 393.70 |
| 62 | I,223,750 | 22,776,3co | 911,050 | $1.713,000$ | 21.974,350 | 414.37 |
| 63 | 1,185,450 | 23,159,800 | 926,390 | 1,800,000 | 22,286,190 | 435.01 |
| 6. | 1145.210 | 23,431,400 | 937,260 | 1,889000 | 22,479,660 | 455.59 |
| 65 | 1,102,480 | 23,582,140 | 943,280 | 1,980,000 | 22,545,420 | 476.03 |
| 66 | I,058.720 | 23,604,140 | 944,160 | 2,070.000 | 22,478,300 | 496.31 |
| 67 | I,O12,450 | 23,490,750 | 939,630 | 2,158,000 | 22,272,380 | 516.36 |
| 68 | 964,210 | 23,236,590 | 929,460 | 2,243,000 | 21,923.050 | 536.15 |
| 69 | 914.070 | 22,837.120 | 913.490 | 2 321,000 | 21,429,610 | 555.62 |
| 70 | 862, 180 | 22,291,790 | 891670 | 2,391,000 | 20,792,460 | 574.73 |
| 71 | 808,740 | 21,601,220 | 864,050 | 2,448,000 | 20,017,270 | 593.45 |
| 72 | 754,010 | 20,771,280 | 830,850 | 2,487,000 | 19,115,130 | 61182 |
| 73 | 698,420 | 19,813,550 | 792,540 | 2,505,000 | 18,101,090 | 629.86 |
| 74 | 642,420 | 18,743,510 | 749.740 | 2,501,000 | 16,992.250 | 64764 |
| 75 | 586,510 | 17,578,760 | 703,150 | 2,476.000 | 15,805,910 | 665:20 |
| 76 | 531,170 | 16,337,100 | 653,480 | 2,431,000 | 14,559,580 | 68258 |
| 77 | 476,830 | 15,036,410 | 601,460 | 2,369,000 | 13,268,870 | 699.79 |
| 78 | 423.870 | 13,692,740 | 547,710 | 2,291,000 | II,949,450 | 716.82 |
| 79 | 372,650 | 12,322,110 | 492,880 | 2,196,000 | 10,618,980 | 733.65 |
| 80 | 323560 | 10,942,540 | 437,700 | 2,091,000 | 9,289,240 | 75097 |
| 81 | 276,820 | 9,566.060 | 382,640 | I 964,000 | 7,984,700 | 766.36 |
| 82 | 232910 | 8,217,610 | 328,700 | I 816,000 | 6730,310 | 782.32 |
| 83 | 192,320 | 6,922,630 | 276,900 | 1,648,000 | 5 551,530 | 798.20 |
| 84 | I55,480 | 5,707,010 | 228.280 | 1.470,000 | 4.465,290 | 81410 |
| 85 | 122,620 | 4,587,910 | 183.520 | 1,292,000 | 3,479.430 | 82982 |
| 86 |  | 3,573.170 | 142,930 | I. II4,000 | 2,602,100 | 84479 |
| 87 | 68,630 | 2,670,730 | 106,830 | 933,000 | 1,844560 | 859.54 |
| 88 | 47,980 | 1,892,540 | 75,900 | 744,000 | 1,224 240 | 87321 |
| 89 | 3I,340 | 1,255,580 | 50,220 | 555,000 | 750,800 | 886.42 |
| 90 | 18,940 | 769,740 | 30,790 | 385,000 | 415.530 | 899.42 |
| 91 | 10,330 | 425,860 | 17.830 | 246,000 | 196,890 | 9 II. 53 |
| 92 | 4,830 | 201,720 | 8.070 | 137000 | 72,790 | 92I. 39 |
| 93 | 1,770 | 74,560 | 2.980 | 58,000 | 19,540 | 93049 |
| 91 | 470 | 26,010 | 800 | 18,000 | 2,810 | 936.67 |
| 95 | 70 | 2,880 | 120 | 3,000 | ...... | 1000.00 |

( I ) shows the total premiums paid by those alive at the beginning of each successive year. Column (2) shows the fund at the beginning of each year just after the premiums have been paid. Column (3) shows the interest on the fund each year. Column (4) shows the death claims in each year. Column (5) shows the fund at the end of each successive year. Column (6) shows the share held for account of each survivor in each successive year (found by dividing the total fund by the number of persons surviving), and this is also the net investment reserve upon each policy.

The functions of the investment reserve will be made clearly apparent by a study of Table No. 4, which has been prepared to illustrate the appropriation each year of the component parts of an ordinary whole life level premium of \$313, paid annually in advance, to secure $\$ 10,000$ at the death of a man now aged 40 years (or, rather, at the end of the year when death occurs). Column ( 1 ) shows the net reserve at the end of each successive year. Column (2) shows the corresponding net amount at risk borne by the company during each successive year. This is always the difference between the face of the policy and the net reserve, which last, being in hand, is not subject to any insurance risks. Column (3) shows the net cost to insure $\$ 10,000$ during each separate year by the scale of natural premiums, as indicated in column (5), Table 1. Column (4) shows the cost to insure the net amounts at risk at the successive ages indicated in the margins. Column (5) shows the deposit portion of the annual premium in each year, which, until the age of 68 is attained in the example given, goes to swell the investment reserve or accumulated deposit. After the age of 68 the yearly costs to insure the net amount at risk exceed the entire net premiums, and hence the deficiencies (as indicated by the minus sign) must be supplied by drawing from the reserve fund.

From the foregoing it will be apparent :
(I.) Every level premium policy is in reality a contract for a yearly decreasing amount of insurance, and a yearly increasing amount of investment. It is a combination of insurance, which is one thing, with investment, which is quite another thing. There is no necessary connection between the two. Insurance or indemnity may be purchased without investment, as investment may be purchased without insurance. The investment element does not add to the security of the insurance, the yearly cost of which depends, under any and every form of policy, upon the net amount at risk borne by the company, and the actual, present, attained age of the person whose life is exposed to mortality. For instance, in the example given (Table No. 4) of a whole life insurance policy of $\$ 10,000$, issued at the age of 40 , the reserve or invested deposits, at the end of twenty years, or at age 60 , 1s $\$ 3,730.35$. Now, this sum is in hand, and is not subject to any insurance hazard, hence the net amount at risk for that year is $\$ 6,269.65$ only. The cost to insure $\$ 10,000$ for one year at age 60 , as shown in column (3), is $\$ 256.67$. Proportionately the cost to insure $\$ 6,269.65$, the net amount at risk, is $\$_{1} 60.9^{2}$, and this is all the insurance done by the company with respect to that policy during that year. At age 70 the net amount at risk is only $\$ 4,254.74$, the cost of which for that year, $\$ 253.50$, is $\$ 29.96$ more than the net an1888 OB Homans Life Insurance Premium and Reserves 20p bonknote

Table No. 4.
Whole Life Insurance by Level or Uniform Premiums. Age at Issue 40 Years Amount Insured $\$ 10,000$. Annual Premium During Life, $\$ 3$ is 3 .

| Age. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\stackrel{(\mathrm{r})}{\$ 135.83}$ | $\begin{gathered} (2) \\ \$ 9,864.12 \end{gathered}$ | (3) \$94.18 | (4) \$92 90 | (5) <br> \$130. 64 | $\begin{gathered} (6) \\ \$ 80.46 \end{gathered}$ | $\begin{gathered} (7) \\ \$ 313.00 \end{gathered}$ |
| 4 | 276.49 | 9,723.51 | 96.23 | 93.59 | 129.95 | 89.46 | 313.00 |
| 42 | 42183 | 9.578.17 | 98.58 | 9442 | 129.12 | 8946 | 313.00 |
| 43 | 572.04 | 9,427.96 | 101.13 | $953+$ | 12820 | 8946 | 313.00 |
| 44 | 726.98 | 9.273 .02 | 104.12 | 9655 | 12699 | 89.46 | 313.00 |
| 45 | 88682 | 9,113.08 | 10734 | 97.82 | 12572 | 89.46 | 3 r 3 co |
| 46 | 1,051.31 | 8,948 69 | 111.17 | 99.48 | 124.06 | 89.46 | 313.00 |
|  | 1,220.50 | 8,779.50 | 11539 | 101.3I | 12223 | 89.46 | $3^{13} 300$ |
|  | 1,394.15 | 8,605.85 | 120.28 | 103.51 | 120.03 | 89.46 | 31300 |
| 49 | r,571.94 | 8,428.06 | 126.02 | 106.21 | 117.33 | 89.46 | 31300 |
| 50. | r.753.66 | 8,246 34 | 13251 | 109. 27 | 11427 | 89.46 | 313.00 |
| 51 | 1,939 03 | 8,060.92 | 139.81 | 112.70 | 110.84 | 89.46 | 313.00 |
| 52 | 2,127.99 | 7.872 .01 | 147.97 | 116.48 | 107.06 | 89.46 | 313.00 |
| 53 | 2,320.16 | 7,679.84 | 15705 | 120.61 | 102.93 | 89.46 | 31300 |
| 54 | 2,515.25 | 7,484 75 | 167.27 | 12520 | 98.34 | 8946 | 313.00 |
|  | 2,713.02 | 7,286.98 | 17857 | 130.12 | 9342 | 8946 | 313.00 |
| 56 | 2.913 .10 | 7,086.90 | 19 I .20 | 135.50 | 8804 | 89.46 | 313.00 |
| 57 | 3.115 .22 | 6.884 .78 | 205.15 | 14 I .24 | $8 \cdot 30$ | 8946 | 313.00 |
| 58 | 3.319 .09 | 6.680 .91 | 220.03 | 147.00 | 76.54 | 89.46 | . 313.00 |
| 59 | 3.524.25 | 6,475.75 | 237.69 | 153.93 | 6961 | 89.46 | 313.00 |
| 60. | 3,730. 35 | 6,269.65 | 256.67 | 160 92 | 62.62 | 89.46 | 31300 |
| 61 | 3.936 .95 | 6,063.05 | 277.69 | 16935 | 5419 | 89.46 | 313.00 |
| 62 | 4,143. 66 | 5,856.34 | 3co 88 | 17620 | 4734 | 8946 | 313.00 |
| 63 | 4.350. 12 | 5.649 .88 | 318.95 | 180.20 | 43.34 | 89.46 | 31300 |
| 64 | 455586 | 5,444.14 | 354.54 | 193.01 | 30.53 | 89.46 | 3 I 300 |
|  | 4,76033 | 5,239.67 | 385.85 | 202.18 | 2136 | 89.46 | 3 I 3 co |
| 66. | 4,963 07 | 5,036.93 | 420,26 | 21168 | tr. 86 | 89.46 | 313.00 |
| 67. | 5.163 64 | 4.836 .36 | 458.15 | 221. 58 | I. 96 | 89,46 | 313.00 |
| 68. | 5.367. 46 | 4.638 .54 | 500.02 | 231.94 | -8.40 | 89.46 | 313.00 |
| 69. | 5,556.16 | 4,443.84 | 545.79 | 24253 | -18.99 | 89.46 | 3 I 300 |
| 70. | 5,747 26 | 4,252.74 | 596.08 | 25350 | -29.96 | 89.46 | 31300 |
| 71 | 5.934.54 | 4,065.46 | 650.63 | 264 6I | -41.07 | 8946 | 313.00 |
| 72 | 6,118 19 | 3.88I.8I | 70897 | 275.23 | -51.69 | 89.46 | 313.00 |
| 73 | 6,298.64 | 3,701. 36 | 77094 | 285.35 | -6I 81 | 89.46 | 313.00 |
| 74 | 6,476.42 | 3,52358 | 836.80 | 294.85 | -71.3I | 8946 | 313.00 |
| 75 | 6,652.02 | 3,347.98 | 907.41 | 303.80 | -80.26 | 8946 | 31300 |
| 76 | 6.825 .83 | 3,174 17 | 98376 | $3{ }^{12} 26$ | -88.72 | 89.46 | 313.00 |
| 77 | 6.99793 | 3,002.07 | 1,067.93 | 320.60 | -97.06 | 89.46 | 313.00 |
| 78 | 7,168.17 | 2,831.83 | 1,161.80 | 329.00 | -105.46 | 89.46 | 313.00 |
| 79 | 7,336.51 | 2,663.49 | r,266.67 | 337.22 | -ri3 68 | 89.46 | 3 I 300 |
| 80 | 7,509.70 | 2,490 30 | r,389 10 |  | -122.36 | 89.46 | 31300 |
| 8 r | 7.66360 | 2.336.40 | 1,525.04 | 356.31 | -132.77 | 89.46 | 313.00 |
| 82 | 7.823 .20 | 2,176.80 | r,675.93 | 364.83 | -I4I 29 | 89.46 | 3 3 3.00 |
| 83 | 7.98200 | 2,018.00 | 1,841.93 | 371.70 | -149 16 | 89.46 | 313.00 |
| 84 | 8 , I4I 00 | 1,85900 | 2,032.30 | 37781 | -r54.27 | 89.46 | 313.00 |
| 85 | 8 298,20 | 1,701.80 | 2,264 92 | 385.44 | -16190 | 89.46 | 313.00 |
| 86 | 8,447.90 | I, 552.40 | 2,554,6 | 396.57 | -173.03 | 89.46 | 313,00 |
| 87 | 8,595.40 | 1,404.60 | 2,913.66 | 409.26 | -185.72 | 89.46 | 3 I 3.00 |
| 88 | 8.732 .10 | 1,267.90 | 3,335.57 | 42261 | -199.07 | 89.46 | 313.00 |
| 89 | 8,864.20 | 1, 135.80 | 3,806.38 | $43^{2} \cdot 3^{2}$ | $-208.78$ | 89.46 | 313.00 |
| 90 | 8,994.20 | I,005 80 | 4,370 63 | 43960 | -216.06 | 8946 | 313.00 |
| 91. | 9,115.30 | 884.70 | 5,119 88 | 452.96 | -229.42 | 89.46 | 313.00 |
| 92. | 9,213.90 | 786. Io | 6,098.68 | 479.42 | -25588 | 89.46 | 313.00 |
| 93 | 9,304.90 | 695, 10 | 7,059.40 | 490.69 | -267.15 | 8946 | 31300 |
|  | 9,366,70 | $633 \cdot 30$ | 8,241.76 | 521.96 | -298.42 | 8946 | 31300 |
| 95.. | 10,000.00 | ...... | 9,615.40 | ...... |  | 89.46 | 313.00 |

nual premium ( $\$ 223.54$ ). The deficiency for that year, as well as the deficiencies for each subsequent year, as shown in column (5), must be met by drawing on the investment reserve, or accumulated fund, the express functions of which is to provide for the excessive cost of insurance in old age when the level premium is insufficient for that purpose.
(2). The investment reserve is occasioned solely by the artificial condition in the level premium contract, which provides that the premiums shall not increase as the insured grows older, and to enable the company to pay the sum insured as an endowment.
(3). Whether the combination of insurance and investment is desirable or advantageous, depends upon the manner in which each is administered. If either the insurance or the investment can be obtained on better terms separately, the combination of the two is certainly undesirable and disadvantageous to the policyholder.

Instead of contracting with a life insurance company for both insurance and investment, which together make up the sum insured, two separate contracts might be made-the one with a life company for the yearly decreasing amounts of insurance only, see column (2) table 4 , the other with a savings bank or trust company for accumulating the deposit, or investment portions of the yearly premium, see column (5) of the same table. In case of death in such case the insurance company would pay the net amount insured only, column (2), while the savings bank would pay the accumulated deposits, column ( $\mathbf{I}$ ), the two together making up the full amount guaranteed.

To show even more clearly how the insurance and investment elements may be completely separated the following tables have been prepared.

Table No. 5 illustrates the case of an endowment assurance issued at age of forty years for $\$ 10,000$ payable in ten years or at death if prior. The net premium only ( $\$ 853.62$ ) is considered-the margin for expenses and adverse contingencies being disregarded.

Tables 6 and 7 are intended to show how the same result can be secured by purchasing a ten-year term insurance with the insurance company, annual premium $\$ 106.03$, and a pure endowment (payable only in case of survival) by depositing the residue (\$747.59) of the endowment assurance premium for accumulation. In case of death at any time during the ten years, the insurance company would pay the full amount insured, and the endowment fund would be lost. In case of surviving, the $\$ 10,000$ would be paid as an endowment, and the insurance would cease.

The same principles apply to any other term of years, as a whole life policy is in reality an endowment assurance payable on attaining the age of ninety-six years, or at death if prior.

Comparison of an endowment assurance contract, a ten year term level premium contract, and a pure endowment contract. Amount $\$ 10,000$, and age at issue 40 years, in each case :

Table No. 5.
Endowment Assurance, Annual Premium \$853.62.

| Year. | Net Reserve or Accumulated 1)eposits Being Self-Insurance. | Net Amount of Insurance at Risk or Carried by the Company. | Tahular Cost Each Year to Insure \$ro,000 for the Year. | Tabular Cost to Insure Net Amount at Risk which is also the Full Legal and Mathematical Insurance Reserve. | Deposit Portion of Annual Premium Which is Merely for Accumulation. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | \$797.63 | \$9,202 37 | \$94. 18 | \$86.67 | \$766 95 |
| 2. | 1,633 57 | 8,366 43 | 9623 | 80.51 | 773.II |
| 3. | 2,509 89 | 7,490.11 | 98.58 | 73.84 | 779.78 |
| 4. | 3,428.95 | 6,571.05 | 101.13 | 6645 | 78717 |
|  | 4,393.16 | 5,606.84 | 104.12 | 58.38 | 795.24 |
|  | 5,405.36 | 4,494 64 | 107.34 | 48.24 | $805 \cdot 38$ |
|  | 6,468.5I | 3,531.49 | III. 17 | 39.26 | 814.36 |
| 8. | 7,586.05 | 2,413.95 | 115.39 | 27.85 | 825.77 |
| 9 | 8,761.76 | 1,238.24 | 120.28 | I4.89 | 838.73 |
| 10 | 10,000.00 | Nıl. | 126.02 | Nil. | 853.62 |

Table No. 6.
Ten-Year Term Insurance, Net Annual Premium \$1o6.03.

| Year. | Net Reserve or Accumulated Deposits Being Self-Insurance. | Net Amount of lnsurance at Risk or Carried by the Company. | Tabular Cost Each Year to Insure \$ro,000 for the Year. | Tabular Cost to Insure Net Amount at Risk which is also the Full Legal and Mathemattical Insurance Reserve. | Deposit Portion of Annual Premium Which is Merely for Accumulation. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | \$12.45 | \$9,987.55 | \$94.18 | \$94.06 | \$11.97 |
| 2. | 23.37 | 9,976.63 | 96.23 | 96.00 | 10.03 |
| 3 | 32.37 | 9,967.63 | 98.58 | 98.26 | 7.77 |
| 4 | 39.18 | 9,960. 82 | IOI.13 | 100.73 | $5 \cdot 30$ |
|  | 43.20 | 9,956.80 | 104.12 | 103.57 | 2.37 |
| 6 | 44.05 | 9,955.95 | 107.34 | 106.87 | -0.84 |
| 7. | 40.95 | 9,959.05 | III.I7 | 110.72 | -4.69 |
| 8 | 33.24 | 9,906.76 | 115.39 | 115.01 | -8.98 |
|  | 19.99 | 9,980 or | 120.28 | 120.04 | -14.01 |
| 10. |  | 10,000.00 | 126.02 | 12602 | -19.99 |

Table No. 7.
Pure Endowment-Age 40 at Issite-\$io,ooo Payable Only in Case of Being Alive at the End of io Years, or at Age 50.

| Year. | Yearly Payments. | Value (Without Interest) of \$r.oo Payable Only in Case of Surviving to End of Year. | Fund at Beginning of Year. | Vauue of Ditto Payable Only in Case of Survivirg. | Interest 4\%. | Fund at End of Year. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | \$747.59 | \$I,009. 89 | \$747.59 | \$754 99 | \$30.20 | \$785. 19 |
| 2 | 747.59 | 1,010.11 | 1,532.78 | I,548.28 | 6I.93 | I,6I0.2I |
| 3 | 747.59 | 1, о10 36 | 2,357.80 | 2,382.23 | 95.29 | 2,477.5I |
|  | 747.59 | 1, ого. 63 | 3,225.10 | 3,259 $3^{8}$ | 130.37 | 3,389 75 |
|  | 747.59 | I,OIO. 95 | 4,137,34 | 4.182 .63 | 167.31 | 4,349.94 |
| 6. | 747.59 | 1,011. 29 | 5,097.53 | 5,155.08 | 206.20 | 5.361.28 |
|  | 747.59 | 1,011.70 | 6,108.87 | 6,180.34 | 247.21 | 6.427.55 |
| 8. | 747.59 | 1,012.15 | 7,175.14 |  | 290.49 |  |
|  | 747.59 | 1,012.67 | 8.300 .40 | 8,405 56 | 336.22 | 8,741.78 |
| 10 | 747.59 | 1,013 28 | 9,489.37 | 9,6I5.39 | 384.61 | 10.000.00 |

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Insurance and investment therefore have no necessary connection-either one may be obtained without the other.
(4). Pure insurance, unmixed with banking or investment, involves the payment of natural premiums, which inevitably and inexorably increase with age. The only way to avoid these increasing rates is to pay largely in excess of the requirements for current death claims in the earlier years, and thus provide a fund upon which to draw in the later years-that is to say, by combining investment with insurance. The first is known as the natural premium plan, the second as the level premium plan. Properly administered, the one is as safe and as sound as the other, as both depend upon the application of the same laws of nature which govern the rates of mortality, or the probability of living and dying in each successive year of life. In fact, as before stated, level premiums are simply the commuted equivalents of the increasing or natural premiums. In both systems, the company must alike be furnished with the cost of insuring the net amount at risk at the actual age attained on each and every policy in force. This cost is independent of the form of policy contract, the age at issue, or the scake of premium charged. This cost, as previously stated, may be furnished either by direct, present payments, as by natural premiums, or partly by direct present payments, and partly by drawing upon the investment reserve or accumulated deposits, a fund contributed by the policyholder for this express purpose.

There are only two sound systems of life insurance; the one by natural premiums, increasing each year as a man grows older; the other, by level premiums, which necessitate investments or accumulated payments largely in excess during the earlier years to meet the deficiencies of the uniform, unchanging premiums in later years. The attempts by so many co-operative or assessment companies to furnish insurance by assessments based upon the age at entry, and which rates do not increase with age must inevitably result in disappointment and disaster. Natural laws may not be violated with impunity.

Sheppard Homans.

New York, May io, 1888.



YD 05532

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$(D) 5 D 2) 55(2) 5 D(2)$

 (2) () Du D $\sum, ~ \ggg>(1, p$
 (2) $25202851,0,2)=3$ - 20 5
(2)

